## 國立交通大學 96 學年度碩士班考試入學試題

科目:普通物理(4012) 考試日期:96年3月18日 第 3 節

系所班別:電子物理學系 組別:電物所甲組 第 1頁,共 2頁

\*\*作答前請先核對試題、答案卷(試卷)與准考證之所組別與考科是否相符!

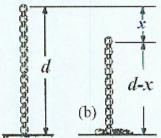
## Part one, single choice: (40%, 每題5%) 不倒扣

- n moles of Ar gas changes from an initial state (P<sub>0</sub>, V<sub>0</sub>, T<sub>0</sub>) to a final state (P<sub>0</sub>/3, 3V<sub>0</sub>, T<sub>0</sub>) by a sudden, irreversible, free expansion. If C<sub>v</sub> and C<sub>p</sub> are the molar specific heats at constant volume and pressure, respectively, and γ = C<sub>v</sub>/C<sub>p</sub>. Then the change of the entropy during this process is (A) 0, (B) nR ln2, (C) nR ln3, (D) γnR ln3, (E) (γ-1)nR ln3.
- A rope of total mass m and length d is suspended vertically. The time t for a transverse wave pulse to travel the entire length of the rope is

(A)  $\sqrt{\frac{d}{g}}$ , (B)  $\sqrt{\frac{2d}{g}}$ , (C)  $2\sqrt{\frac{d}{g}}$ , (D)  $\sqrt{\frac{d}{2g}}$ , (E)  $\frac{1}{2}\sqrt{\frac{d}{g}}$ .

3. A chain of length d and total mass m is released from rest with its lower end just touching the top of a table, as in Figure 1a. Assume each link comes to rest the instant it reaches the table, then the force exerted by the table on the chain after the chain has fallen through a distance x, as in Figure 1b, is

(A)  $\frac{3mgx}{d}$ , (B)  $\frac{2mgx}{d}$ , (C)  $\frac{mgx}{d}$ , (D)  $\frac{mgx}{3d}$ , (E)  $\frac{3mgx}{2d}$ .



4. The potential energy of the two atoms in a diatomic (two-atom) molecule can be written
U(r) = -\frac{a}{r^6} + \frac{b}{r^{12}} \text{ where } r \text{ is the distance between the two atoms and } a \text{ and } b \text{ are positive constants. The binding energy of a two-particle system is defined as the energy required to separate the two particles from their state of lowest energy to r = ∞. Find the binding energy for the molecule:

Figure 1 (a)

(A) 
$$\frac{a^2}{2b}$$
, (B)  $\frac{2a^2}{b}$ , (C)  $\frac{4a^2}{b}$ , (D)  $\frac{a^2}{4b}$ , (E)  $\frac{a^2}{b}$ .

5. A rod of length L has a total charge Q uniformly distributed over the rod. Find the force acting by Q on a charge q, which is located along the long axis of the rod and a distance d from one end of the rod.

(A)  $q(Q/L)/(4\pi\epsilon_0 d)$ , (B)  $qQ/[4\pi\epsilon_0 L(L+d)]$ , (C)  $q(Q/L)/[4\pi\epsilon_0 L(L+d)]$ , (D)  $qQ/[4\pi\epsilon_0 d(L+d)]$ , (E)  $qQ/(\epsilon_0 dL)$ .

6. What is the capacitance of an isolated charged metal sphere which has radius R? (A) 4πRε<sub>0</sub>, (B) R/4πε<sub>0</sub>, (C) (4π/3)R<sup>3</sup>ε<sub>0</sub>, (D) 4πR<sup>2</sup>ε<sub>0</sub>, (E) 4πR<sup>2</sup>/ε<sub>0</sub>.

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7. Molybdenum has a work function of 4.20 eV. What is the stopping potential if the incident light has a wavelength of 200 nm?

(A) 26 V, (B) 8.4 V, (C) 2.0 V, (D) 1.0 V, (E) 0.1 V.

8. A student uses a microscope to observe micro-structures. The wavelength of the illumination light is 600 nm. The aperture of the objective has a diameter of 1.22 cm. What is the limiting angle of resolution?

(A) 2 degree, (B) 5×10<sup>-5</sup> degree, (C) 6×10<sup>-5</sup> rad, (D) 732 rad, (E) 2×10<sup>5</sup> rad.

Part two, problems: (60%, 每題 15%)

- 9. A solid sphere of radius R and mass M is placed in a cylindrical trough (radius = 5R), as shown in Figure 2. The sphere is released from rest at a small angle θ<sub>0</sub> to the vertical and rolls without slipping. The rolling direction is perpendicular to the length of the trough.
- (a) **Show** that the magnitude of the angular speed of the sphere can be expressed as  $|\omega| = 4 \frac{d\theta}{dt}$  (3%).
- (b) Determine the angular speed of the sphere when it reaches the bottom of the trough (3%).

(c) Find the equation of motion for  $\theta$  (5%).

(d) Show that the sphere executes simple harmonic motion and find the period T of the simple harmonic motion. (4%)

Notes: (1) The moment of the inertia of a solid sphere about its symmetry axis is  $I = 2/5 MR^2$ .

(2) 
$$\sin \theta = \theta - \theta^3/3! + \theta^5/5! - \cdots$$
  
 $\cos \theta = 1 - \theta^2/2! + \theta^4/4! - \cdots$ 

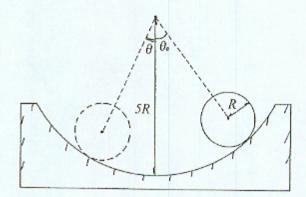


Figure 2

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- 10. Suppose a person of mass  $m = 6.5 \times 10^1 \, kg$  is running at a speed  $v = 3.8 \, m/s$  and has a catabolic (分解代謝) power output (that is, rate of internal energy consumption)  $9.45 \times 10^2 W$  during a  $1.0 \times 10^1 \, km$  workout. Suppose the runner converts 20% of the internal energy change into mechanical work. The rest of the energy goes into heat. If the specific heat of the runner is  $c = 4.19 \times 10^3 \, J \, kg K$ , how much would the body temperature rise after running the  $10 \, km$ ? (15%)
- 11. A series *RLC* circuit has  $R = 200 \ \Omega$ ,  $L = 250 \ \text{mH}$ , and  $C = 10.0 \ \mu\text{F}$ . The applied voltage has an amplitude of 50.0 V and an angular frequency ( $\omega$ ) of 1000 Hz. Find the following amplitudes: (a) The current  $I_{\text{max}}$ , (b) the voltage  $\Delta Vc$  across the capacitor and its phase relative to the current, and (c) the voltage  $\Delta Vc$  across the inductor and its phase relative to the current.(15%)
- 12. A conducting rod of length  $\ell$  moves with velocity v(t)=5t (m/s) parallel to a long wire carrying a steady current I, where t is in second. The axis of the rod is maintained perpendicular to the wire with the near end a distance r (=  $\ell$ ) away. Find the emf induced in the rod at t=3 second. (15%)