

Chapter 1

Binary Search

a: element list

x: the element to be searched.

left, right: the left and right ends of the list

Iterative Binary Search (對應課本程式 Program 1.7)

```
initialize left and right;  
while(there are more integers to check)    // ____ ≤ ____  
{  
    let a[middle] be the middle element;    // middle = ____  
    switch(COMPARE(x, a[middle]))  
    {  
        case '>':    left = middle + 1;  
                   break;  
        case '=':    return middle;  
        case '<':    right = middle - 1;  
    }  
}  
return -1;
```

Recursive Binary Search (對應課本程式 Program 1.8)

n: the number of elements in the list

```
int BinarySearch(list, search_num, left, right)  
{  
    int middle;  
    if(left <= right)    // terminate condition  
    {  
        middle = (left + right) / 2;  
        switch(COMPARE(search_num, list[middle]))  
        {  
            case '>':    return BinarySearch(list, search_num, middle + 1, right);  
            case '=':    return middle;  
            case '<':    return BinarySearch(list, search_num, left, middle - 1);  
        }  
    }  
    return -1;  
}
```

change of
parameters

BinarySearch(a, x, 0, n - 1);

Chapter 2

Polynomial

Polynomial Addition (Array)

```
polynomial add_p(polynomial a, polynomial b)
{
    polynomial c;
    int m_degree;

    m_degree = MAX(a.degree, b.degree);
    for(i = 0; i <= m_degree; i++)
        c.coef[i] = a.coef[i] + b.coef[i];

    c.degree = m_degree;
}
```

Polynomial Addition (Linked List) (對應課本程式 Program 2.6)

p : points to the first element of polynomial *a*

q : points to the first element of polynomial *b*

```
while(!IS_ZERO(p) && !IS_ZERO(q))
{
    switch(COMPARE(EXP_OF(p), EXP_OF(q)))
    {
        case '>':    attach p to c;
                     advance p to the next element in a;
                     break;

        case '<':    attach q to c;
                     advance q to the next element in b;
                     break;

        case '=':    add the coefficients of p and q;
                     attach to c;
                     advance p to the next element in a;
                     advance q to the next element in b;
    }
}

if(there are remaining terms in a)
    attach all of them to c;

if(there are remaining terms in b)
    attach all of them to c;
```

Matrix (2D-Array)

Transpose

a : $m \times n$ matrix

c : $n \times m$ matrix

$$c \leftarrow \text{transpose}(a)$$

```

for( $i = 0; i < m; i++$ )           //  $O(m)$ 
    for( $j = 0; j < n; j++$ )        //  $O(n)$ 
         $c[j][i] = a[i][j];$ 

```

$O(m \cdot n)$

Addition

$a, b, c: m \times n$ matrices

$$c \leftarrow \text{add}(a, b)$$

```
for(i = 0; i < m; i++) // O(m)
    for(j = 0; j < n; j++) // O(n)
        c[i][j] = a[i][j] + b[i][j];
```

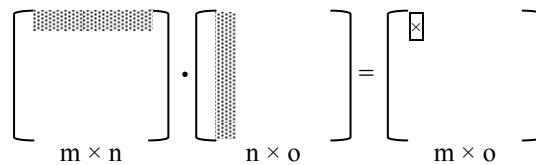
O(m • n)

Multiplication

a : $m \times n$ matrix

b : $n \times o$ matrix

c: $m \times o$ matrix

$$c \leftarrow \text{multiply}(a, b)$$


```

for( $i = 0; i < m; i++$ )                                // O(m)
    for( $j = 0; j < o; j++$ )                                // O(o)
    {
         $sum = 0;$ 
        for( $k = 0; k < n; k++$ )                            // O(n)
             $sum = sum + a[i][k] * b[k][j];$ 
         $c[i][j] = sum;$ 
    }

```

$O(m \cdot n \cdot o)$

$$O(m \cdot n \cdot o)$$

Sparse Matrix (1D Array)

Fast Transpose (對應課本程式 Program 2.9)

$b \leftarrow \text{transpose}(a)$

```
FastTranspose(term  $a[]$ , term  $b[]$ )
{
    initialize  $b[0]$ ;
    initialize  $\text{row\_terms}[]$  to  $\emptyset$ ;

    for( $i = 0$ ;  $i \leq \#terms$ ;  $i++$ )
    {
        // compute row size
         $\text{row\_terms}[a[i].col] = \text{row\_terms}[a[i].col] + 1$ ;
    }

    compute  $\text{row\_start}[]$ ;

    for( $i = 1$ ;  $i \leq \#terms$ ;  $i++$ )
    {
        assign data in  $a[i]$  to  $b[\text{row\_start}[a[i].col]]$ ;
         $\text{row\_start}[a[i].col] = \text{row\_start}[a[i].col] + 1$ ;
    }
}
```

$O(\#terms + \#col)$